Eureka Math Grade 4 Module 5

Published by Great Minds®.

Copyright © 2018 Great Minds®...

Printed in the U.S.A. This book may be purchased from the publisher at eureka-math.org. 10 $\,$ 9 $\,$ 8 $\,$ 7 $\,$ 6 $\,$ 5 $\,$ 4 $\,$ 3

ISBN 978-1-64054-068-2

G4-M5-L-05.2018

Learn + Practice + Succeed

Eureka Math® student materials for A Story of Units® (K–5) are available in the Learn, Practice, Succeed trio. This series supports differentiation and remediation while keeping student materials organized and accessible. Educators will find that the Learn, Practice, and Succeed series also offers coherent—and therefore, more effective—resources for Response to Intervention (RTI), extra practice, and summer learning.

Learn

Eureka Math Learn serves as a student's in-class companion where they show their thinking, share what they know, and watch their knowledge build every day. Learn assembles the daily classwork—Application Problems, Exit Tickets, Problem Sets, templates—in an easily stored and navigated volume.

Practice

Each *Eureka Math* lesson begins with a series of energetic, joyous fluency activities, including those found in *Eureka Math Practice*. Students who are fluent in their math facts can master more material more deeply. With *Practice*, students build competence in newly acquired skills and reinforce previous learning in preparation for the next lesson.

Together, *Learn* and *Practice* provide all the print materials students will use for their core math instruction.

Succeed

Eureka Math Succeed enables students to work individually toward mastery. These additional problem sets align lesson by lesson with classroom instruction, making them ideal for use as homework or extra practice. Each problem set is accompanied by a Homework Helper, a set of worked examples that illustrate how to solve similar problems.

Teachers and tutors can use *Succeed* books from prior grade levels as curriculum-consistent tools for filling gaps in foundational knowledge. Students will thrive and progress more quickly as familiar models facilitate connections to their current grade-level content.



Students, families, and educators:

Thank you for being part of the *Eureka Math*® community, where we celebrate the joy, wonder, and thrill of mathematics.

In the *Eureka Math* classroom, new learning is activated through rich experiences and dialogue. The *Learn* book puts in each student's hands the prompts and problem sequences they need to express and consolidate their learning in class.

What is in the Learn book?

Application Problems: Problem solving in a real-world context is a daily part of *Eureka Math*. Students build confidence and perseverance as they apply their knowledge in new and varied situations. The curriculum encourages students to use the RDW process—Read the problem, Draw to make sense of the problem, and Write an equation and a solution. Teachers facilitate as students share their work and explain their solution strategies to one another.

Problem Sets: A carefully sequenced Problem Set provides an in-class opportunity for independent work, with multiple entry points for differentiation. Teachers can use the Preparation and Customization process to select "Must Do" problems for each student. Some students will complete more problems than others; what is important is that all students have a 10-minute period to immediately exercise what they've learned, with light support from their teacher.

Students bring the Problem Set with them to the culminating point of each lesson: the Student Debrief. Here, students reflect with their peers and their teacher, articulating and consolidating what they wondered, noticed, and learned that day.

Exit Tickets: Students show their teacher what they know through their work on the daily Exit Ticket. This check for understanding provides the teacher with valuable real-time evidence of the efficacy of that day's instruction, giving critical insight into where to focus next.

Templates: From time to time, the Application Problem, Problem Set, or other classroom activity requires that students have their own copy of a picture, reusable model, or data set. Each of these templates is provided with the first lesson that requires it.

Where can I learn more about Eureka Math resources?

The Great Minds® team is committed to supporting students, families, and educators with an ever-growing library of resources, available at eureka-math.org. The website also offers inspiring stories of success in the *Eureka Math* community. Share your insights and accomplishments with fellow users by becoming a *Eureka Math* Champion.

Best wishes for a year filled with aha moments!

Jill Diniz

Director of Mathematics Great Minds

Till Ding

The Read-Draw-Write Process

The Eureka Math curriculum supports students as they problem-solve by using a simple, repeatable process introduced by the teacher. The Read–Draw–Write (RDW) process calls for students to

- 1. Read the problem.
- 2. Draw and label.
- 3. Write an equation.
- 4. Write a word sentence (statement).

Educators are encouraged to scaffold the process by interjecting questions such as

- What do you see?
- Can you draw something?
- What conclusions can you make from your drawing?

The more students participate in reasoning through problems with this systematic, open approach, the more they internalize the thought process and apply it instinctively for years to come.

					1
	18				

Contents

Module 5: Fraction Equivalence, Ordering, and Operations

Topic A: Decomposition and Fraction Equivalence	
Lesson 1	a ta estado. 1
Lesson 2	
Lesson 3	15
Lesson 4	21
Lesson 5	29
Lesson 6	
Topic B: Fraction Equivalence Using Multiplication and Division	
Lesson 7	
Lesson 8	51
Lesson 9	57
Lesson 10	65
Lesson 11	73
Topic C: Fraction Comparison	
Lesson 12	pt to the second 81
Lesson 13	· ** *** ******** 89
Lesson 14	97
Lesson 15	
Topic D: Fraction Addition and Subtraction	
Lesson 16	113
Lesson 17	
Lesson 18	
Lesson 19	
Lesson 20	
Lesson 21	

Topic E: Extending Fraction Equivalence to Fractions Greater Than 1	
Lesson 22	51
Lesson 23	57
Lesson 24	33
Lesson 25	39
Lesson 26	75
Lesson 27	31
Lesson 28	37
Topic F: Addition and Subtraction of Fractions by Decomposition	
Lesson 29	3 1
Lesson 30	3 7
Lesson 31)5
Lesson 32	11
Lesson 33	17
Lesson 34	23
Topic G: Repeated Addition of Fractions as Multiplication	
Lesson 35	29
Lesson 36	35
Lesson 37	11
Lesson 38	17
Lesson 39	53
Lesson 40	57
Topic H: Exploring a Fraction Pattern	
Lesson 41	31

			_	
	rs to cut an index card on the		. Prove that you have	cut the rectangle
into 4 fourths.	Include a drawing in your ex	planation.		
				-
		_		
	Read	Draw	Write	



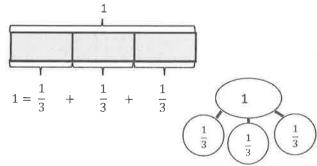
Lesson 1:

Decompose fractions as a sum of unit fractions using tape diagrams.

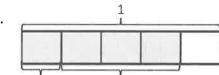
					٠
				9	

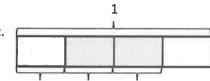
1. Draw a number bond, and write the number sentence to match each tape diagram. The first one is done for you.

a.

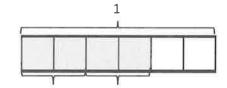


b.

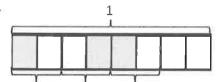




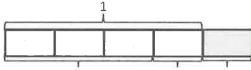
d.



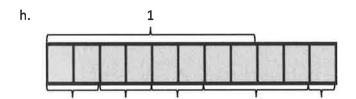
e.



f.







2. Draw and label tape diagrams to model each decomposition.

a.
$$1 = \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6}$$

$$b_{ij} \frac{4}{5} = \frac{1}{5} + \frac{2}{5} + \frac{1}{5}$$

c.
$$\frac{7}{8} = \frac{3}{8} + \frac{3}{8} + \frac{1}{8}$$

$$d_{-1} = \frac{11}{8} = \frac{7}{8} + \frac{1}{8} + \frac{3}{8}$$

e.
$$\frac{12}{10} = \frac{6}{10} + \frac{4}{10} + \frac{2}{10}$$

f.
$$\frac{15}{12} = \frac{8}{12} + \frac{3}{12} + \frac{4}{12}$$

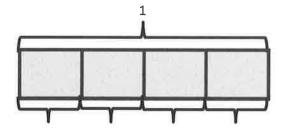
g.
$$1\frac{2}{3} = 1 + \frac{2}{3}$$

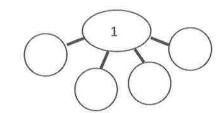
$$h_0 \ 1\frac{5}{8} = 1 + \frac{1}{8} + \frac{1}{8} + \frac{3}{8}$$



			Y.
8			

1. Complete the number bond, and write the number sentence to match the tape diagram.





2. Draw and label tape diagrams to model each number sentence.

a.
$$1 = \frac{1}{5} + \frac{1}{5} + \frac{1}{5} + \frac{1}{5} + \frac{1}{5}$$

$$b. \ \frac{5}{6} = \frac{2}{6} + \frac{2}{6} + \frac{1}{6}$$

			ĸ

Mrs. Salcido cut a small birthday cake into 6 equal pieces for 6 children. One child was not hungry, so she gave the birthday boy the extra piece. Draw a tape diagram to show how much cake each of the five children received.

Draw

Write

Lesson 2:

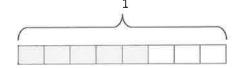
Read

Date _____

- 1. Step 1: Draw and shade a tape diagram of the given fraction.
 - Step 2: Record the decomposition as a sum of unit fractions.
 - Step 3: Record the decomposition of the fraction two more ways.

(The first one has been done for you.)

a.



$$\frac{5}{8} = \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8}$$

$$\frac{5}{8} = \frac{2}{8} + \frac{2}{8} + \frac{1}{8}$$

$$\frac{5}{8} = \frac{2}{8} + \frac{1}{8} + \frac{$$

$$\frac{5}{8} = \frac{2}{8} + \frac{2}{8} + \frac{1}{8}$$

$$\frac{5}{8} = \frac{2}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8}$$

b.
$$\frac{9}{10}$$

c.
$$\frac{3}{2}$$

- 2. Step 1: Draw and shade a tape diagram of the given fraction.
 - Step 2: Record the decomposition of the fraction in three different ways using number sentences.

b. $\frac{5}{3}$

c. $\frac{7}{5}$

d. 1_3^1

© 2018 Great Minds®. eureka-math.org

Name	Date

- Step 1: Draw and shade a tape diagram of the given fraction.
- Step 2: Record the decomposition of the fraction in three different ways using number sentences.

 $\frac{4}{7}$



Mrs. Beach prepared copies for 4 reading groups. She made 6 copies for each group. How many copies did Mrs. Beach make?

a. Draw a tape diagram.

b. Write both an addition and a multiplication sentence to solve.

Read

Draw

Write



c. What fraction of the copies is needed for 3 groups? To show that, shade the tape diagram.

Read

Draw

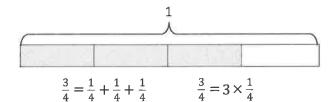
Write

Name _____

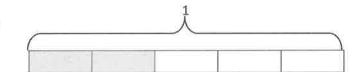
Date _____

1. Decompose each fraction modeled by a tape diagram as a sum of unit fractions. Write the equivalent multiplication sentence. The first one has been done for you.

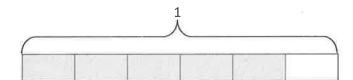
a.



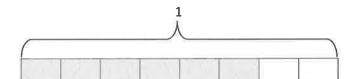
b.



c.



d.



e.



2. Write the following fractions greater than 1 as the sum of two products.

1 a.

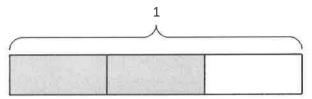
b.

- 3. Draw a tape diagram, and record the given fraction's decomposition into unit fractions as a multiplication sentence.
 - a. $\frac{4}{5}$
 - b. $\frac{5}{8}$
 - c. $\frac{7}{9}$
 - d. $\frac{7}{4}$
 - e. $\frac{7}{6}$

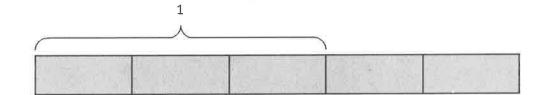
Name ______

1. Decompose each fraction modeled by a tape diagram as a sum of unit fractions. Write the equivalent multiplication sentence.

a.



b.



2. Draw a tape diagram, and record the given fraction's decomposition into unit fractions as a multiplication sentence.

 $\frac{6}{9}$

A recipe calls for $\frac{3}{4}$ cup of milk. Saisha only has a $\frac{1}{4}$ -cup measuring cup. If she doubles the recipe, how many times will she need to fill the $\frac{1}{4}$ cup with milk? Draw a tape diagram, and record as a multiplication sentence.

Read

Draw

Write



Lesson 4:

Decompose fractions into sums of smaller unit fractions using tape diagrams.

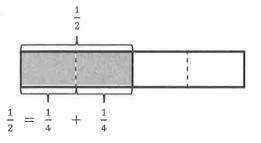
*			
	*		

Name__

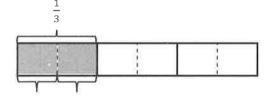
Date _____

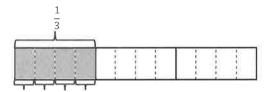
1. The total length of each tape diagram represents 1. Decompose the shaded unit fractions as the sum of smaller unit fractions in at least two different ways. The first one has been done for you.

a.



b.





c.





d.





2. The total length of each tape diagram represents 1. Decompose the shaded fractions as the sum of smaller unit fractions in at least two different ways.

a.



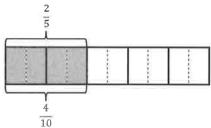
b.





3. Draw and label tape diagrams to prove the following statements. The first one has been done for you.

a.
$$\frac{2}{5} = \frac{4}{10}$$



b.
$$\frac{2}{6} = \frac{4}{12}$$

c. $\frac{3}{4} = \frac{6}{8}$

- d. $\frac{3}{4} = \frac{9}{12}$
- 4. Show that $\frac{1}{2}$ is equivalent to $\frac{4}{8}$ using a tape diagram and a number sentence.

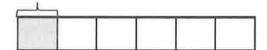
5. Show that $\frac{2}{3}$ is equivalent to $\frac{6}{9}$ using a tape diagram and a number sentence.

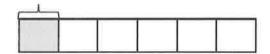
6. Show that $\frac{4}{6}$ is equivalent to $\frac{8}{12}$ using a tape diagram and a number sentence.

		25	

Name _____

1. The total length of the tape diagram represents 1. Decompose the shaded unit fraction as the sum of smaller unit fractions in at least two different ways.





2. Draw a tape diagram to prove the following statement.

$$\frac{2}{3} = \frac{4}{6}$$

A loaf of bread was cut into 6 equal slices. Each of the 6 slices was cut in half to make thinner slices for sandwiches. Mr. Beach used 4 slices. His daughter said, "Wow! You used $\frac{2}{6}$ of the loaf!" His son said, "No. He used $\frac{4}{12}$." Explain who was correct using a tape diagram.

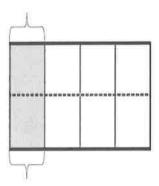
Draw

Write

Lesson 5:

Read

- 1. Draw horizontal lines to decompose each rectangle into the number of rows as indicated. Use the model to give the shaded area as both a sum of unit fractions and as a multiplication sentence.
 - a. 2 rows

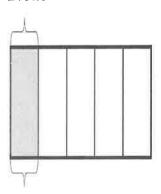


$$\frac{1}{4} = \frac{2}{}$$

$$\frac{1}{4} = \frac{1}{8} + \dots = \dots$$

$$\frac{1}{4} = 2 \times - = -$$

b. 2 rows



c. 4 rows



2. Draw area models to show the decompositions represented by the number sentences below. Represent the decomposition as a sum of unit fractions and as a multiplication sentence.

a.
$$\frac{1}{2} = \frac{3}{6}$$

b.
$$\frac{1}{2} = \frac{4}{8}$$

C.
$$\frac{1}{2} = \frac{5}{10}$$

d.
$$\frac{1}{3} = \frac{2}{6}$$

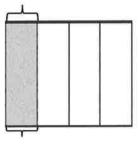
e.
$$\frac{1}{3} = \frac{4}{12}$$

$$f_{1} = \frac{1}{4} = \frac{3}{12}$$

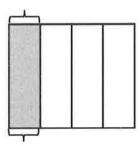
3. Explain why $\frac{1}{12} + \frac{1}{12} + \frac{1}{12}$ is the same as $\frac{1}{4}$.

Name	Date

- 1. Draw horizontal lines to decompose each rectangle into the number of rows as indicated. Use the model to give the shaded area as both a sum of unit fractions and as a multiplication sentence.
 - a. 2 rows



b. 3 rows



2. Draw an area model to show the decomposition represented by the number sentence below. Represent the decomposition as a sum of unit fractions and as a multiplication sentence.

$$\frac{3}{5} = \frac{6}{10}$$



	8	

Use area models to prove that $\frac{1}{2}=\frac{2}{4}=\frac{4}{8}$, $\frac{1}{2}=\frac{3}{6}=\frac{6}{12}$, and $\frac{1}{2}=\frac{5}{10}$. What conclusion can you make about $\frac{4}{8}$, $\frac{6}{12}$, and $\frac{5}{10}$? Explain.

Read

Draw

Write

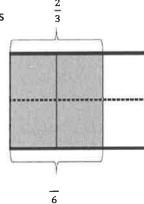


Lesson 6:

Decompose fractions using area models to show equivalence.

Date ___

- Each rectangle represents 1. Draw horizontal lines to decompose each rectangle into the fractional units as indicated. Use the model to give the shaded area as a sum and as a product of unit fractions. Use parentheses to show the relationship between the number sentences. The first one has been partially done for you.
 - a. Sixths



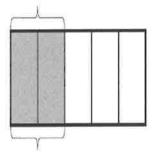
$$\frac{2}{3} = \frac{4}{3}$$

$$\frac{2}{3} + \frac{1}{3} = \left(\frac{1}{6} + \frac{1}{6}\right) + \left(\frac{1}{6} + \frac{1}{6}\right) = \frac{4}{6}$$

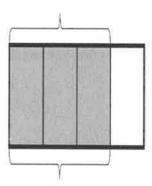
$$\left(\frac{1}{6} + \frac{1}{6}\right) + \left(\frac{1}{6} + \frac{1}{6}\right) = \left(2 \times -\right) + \left(2 \times -\right) = \frac{4}{3}$$

$$\frac{2}{3} = 4 \times - = \frac{4}{3}$$

b. Tenths



c. Twelfths



2. Draw area models to show the decompositions represented by the number sentences below. Express each as a sum and product of unit fractions. Use parentheses to show the relationship between the number sentences.

a.
$$\frac{3}{5} = \frac{6}{10}$$

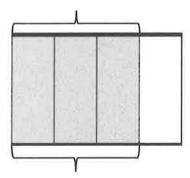
b.
$$\frac{3}{4} = \frac{6}{8}$$

© 2018 Great Minds®. eureka-math.org

- 3. Step 1: Draw an area model for a fraction with units of thirds, fourths, or fifths.
 - Step 2: Shade in more than one fractional unit.
 - Step 3: Partition the area model again to find an equivalent fraction.
 - Step 4: Write the equivalent fractions as a number sentence. (If you've written a number sentence like this one already on this Problem Set, start over.)



1. The rectangle below represents 1. Draw horizontal lines to decompose the rectangle into eighths. Use the model to give the shaded area as a sum and as a product of unit fractions. Use parentheses to show the relationship between the number sentences.



2. Draw an area model to show the decomposition represented by the number sentence below.

$$\frac{4}{5} = \frac{8}{10}$$

Model an equivalent fraction for $\frac{4}{7}$ using an area model.

Read

Draw

Write



Lesson 7:

Use the area model and multiplication to show the equivalence of two fractions.

Name _____

Each rectangle represents 1.

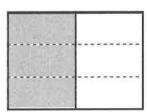
1. The shaded unit fractions have been decomposed into smaller units. Express the equivalent fractions in a number sentence using multiplication. The first one has been done for you.

a.

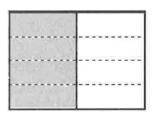


$$\frac{1}{2} = \frac{1 \times 2}{2 \times 2} = \frac{2}{4}$$

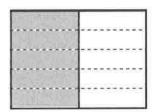
b.



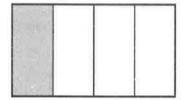
C.



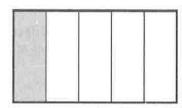
d.



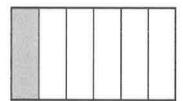
2. Decompose the shaded fractions into smaller units using the area models. Express the equivalent fractions in a number sentence using multiplication.



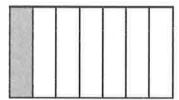
b.



C.,



d.



What happened to the size of the fractional units when you decomposed the fraction?

f. What happened to the total number of units in the whole when you decomposed the fraction?

3. Draw three different area models to represent 1 third by shading. Decompose the shaded fraction into (a) sixths, (b) ninths, and (c) twelfths. Use multiplication to show how each fraction is equivalent to 1 third.

a.

b.

c.



Name	Date	

Draw two different area models to represent 1 fourth by shading. Decompose the shaded fraction into (a) eighths and (b) twelfths. Use multiplication to show how each fraction is equivalent to 1 fourth.

a.

b.



Saisha gives some of her chocolate bar, pictured below, to her younger brother Lucas. He says, "Thanks for $\frac{3}{12}$ of the bar." Saisha responds, "No. I gave you $\frac{1}{4}$ of the bar." Explain why both Lucas and Saisha are correct.



	R	ead	Draw	Write	
UREKA	Lesson 8:	Use the area fractions.	model and multiplication	to show the equivalence of tw	vo

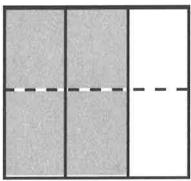
© 2018 Great Minds®. eureka-math.org

Name _

Each rectangle represents 1.

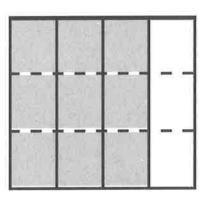
1. The shaded fractions have been decomposed into smaller units. Express the equivalent fractions in a number sentence using multiplication. The first one has been done for you.

a.

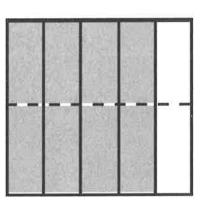


$$\frac{2}{3} = \frac{2 \times 2}{3 \times 2} = \frac{4}{6}$$

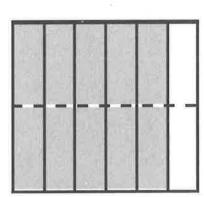
b.



c.

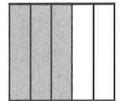


d.

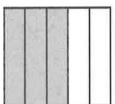


Decompose the shaded fractions into smaller units, as given below. Express the equivalent fractions in a number sentence using multiplication.

Decompose into tenths.



Decompose into fifteenths.



3. Draw area models to prove that the following number sentences are true.

$$a_{*}$$
 $\frac{2}{5} = \frac{4}{10}$

b.
$$\frac{2}{3} = \frac{8}{12}$$

c.
$$\frac{3}{6} = \frac{6}{12}$$

d.
$$\frac{4}{6} = \frac{8}{12}$$

4. Use multiplication to find an equivalent fraction for each fraction below.

a.
$$\frac{3}{4}$$

b.
$$\frac{4}{5}$$

c.
$$\frac{7}{6}$$

d.
$$\frac{12}{7}$$

5. Determine which of the following are true number sentences. Correct those that are false by changing the right-hand side of the number sentence.

a.
$$\frac{4}{3} = \frac{8}{9}$$

b.
$$\frac{5}{4} = \frac{10}{8}$$

c.
$$\frac{4}{5} = \frac{12}{10}$$

d.
$$\frac{4}{6} = \frac{12}{18}$$

© 2018 Great Minds®. eureka-math.org

Name _____ Date _____

1. Use multiplication to create an equivalent fraction for the fraction below.

<u>2</u> 5

2. Determine if the following is a true number sentence. If needed, correct the statement by changing the right-hand side of the number sentence.

 $\frac{3}{4} = \frac{9}{8}$

What fraction of a foot is 1 in Draw a tape diagram to most		on of a foot is 3 incl	hes? (Hint: 12 inches = 1 foot.)
	Read	Draw	Write



Lesson 9:

Use the area model and division to show the equivalence of two fractions.

Name ______

Date _____

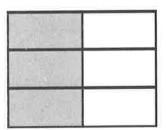
Each rectangle represents 1.

1. Compose the shaded fractions into larger fractional units. Express the equivalent fractions in a number sentence using division. The first one has been done for you.

a.



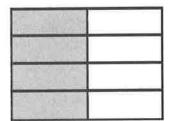
b.



c.

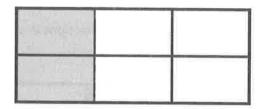


d.

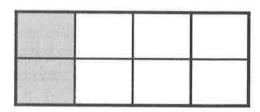


2. Compose the shaded fractions into larger fractional units. Express the equivalent fractions in a number sentence using division.

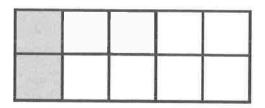
a.



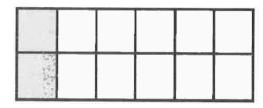
b.



c.



d.



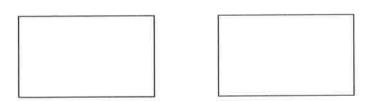
e. What happened to the size of the fractional units when you composed the fraction?

What happened to the total number of units in the whole when you composed the fraction?



3. a.		In the first area model, show 2 sixths. In the second area model, show 3 ninths. Show how both fractions can be renamed as the same unit fraction.					
	b.	Express the equivalent fractions in a number sentence using division.					

4. a. In the first area model, show 2 eighths. In the second area model, show 3 twelfths. Show how both fractions can be composed, or renamed, as the same unit fraction.



b. Express the equivalent fractions in a number sentence using division.



Name _.	Date					
a.	In the first area model, show 2 sixths. In the second area model, show 4 twelfths. Show how be fractions can be composed, or renamed, as the same unit fraction.					

b. Express the equivalent fractions in a number sentence using division.



Nuri spent $\frac{9}{12}$ of his money on a book and the rest of his money on a pencil.

a. Express how much of his money he spent on the pencil in fourths.

b. Nuri started with \$1. How much did he spend on the pencil?

Read

Draw

Write



	D.	

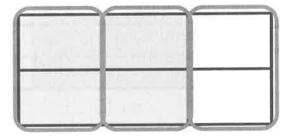
Name ______

Date _____

Each rectangle represents 1.

1. Compose the shaded fraction into larger fractional units. Express the equivalent fractions in a number sentence using division. The first one has been done for you.

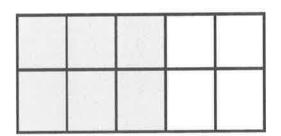
a.



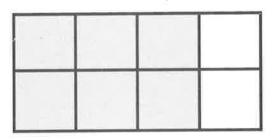
b.

3.17	

c.



d.



Name	Date	
NO 45 AM (AMOS)		_

Draw an area model to show why the fractions are equivalent. Show the equivalence in a number sentence using division.

$$\frac{4}{10} = \frac{2}{5}$$



Kelly was baking bread but could only find her $\frac{1}{8}$ -cup measuring cup. She needs $\frac{1}{4}$ cup sugar,
$\frac{3}{4}$ cup whole wheat flour, and $\frac{1}{2}$ cup all-purpose flour. How many $\frac{1}{8}$ cups will she need for each
ingredient?

Read

Draw

Write



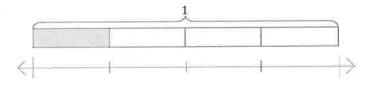
Lesson 11:

Explain fraction equivalence using a tape diagram and the number line, and relate that to the use of multiplication and division.

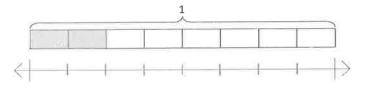
Namo	Date
Name	Date

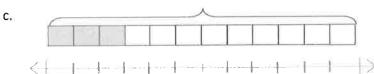
1. Label each number line with the fractions shown on the tape diagram. Circle the fraction that labels the point on the number line that also names the shaded part of the tape diagram.

a.



b.

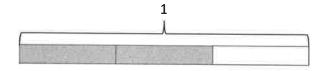






- 2. Write number sentences using multiplication to show:
 - a. The fraction represented in 1(a) is equivalent to the fraction represented in 1(b).
 - b. The fraction represented in 1(a) is equivalent to the fraction represented in 1(c).
- 3. Use each shaded tape diagram below as a ruler to draw a number line. Mark each number line with the fractional units shown on the tape diagram, and circle the fraction that labels the point on the number line that also names the shaded part of the tape diagram.

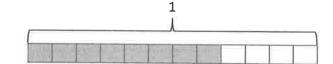
a.



b.



c.



- Write number sentences using division to show:
 - a. The fraction represented in 3(a) is equivalent to the fraction represented in 3(b).
 - b. The fraction represented in 3(a) is equivalent to the fraction represented in 3(c).

- 5. a. Partition a number line from 0 to 1 into fifths. Decompose $\frac{2}{5}$ into 4 equal lengths.
 - b. Write a number sentence using multiplication to show what fraction represented on the number line is equivalent to $\frac{2}{5}$.
 - c. Write a number sentence using division to show what fraction represented on the number line is equivalent to $\frac{2}{5}$.



	,		

Name	Date
Name	

1. Partition a number line from 0 to 1 into sixths. Decompose $\frac{2}{6}$ into 4 equal lengths.

2. Write a number sentence using multiplication to show what fraction represented on the number line is equivalent to $\frac{2}{6}$

3. Write a number sentence using division to show what fraction represented on the number line is equivalent to $\frac{2}{6}$.



Plot $\frac{1}{4}$, $\frac{4}{5}$, and $\frac{5}{8}$ on a number line, and compare the three points.

Read

Draw

Write



Lesson 12:

Reason using benchmarks to compare two fractions on the number line.

	5		*	

- 1. a. Plot the following points on the number line without measuring.
 - $1. \frac{1}{3}$

iii. $\frac{7}{12}$



b. Use the number line in Part (a) to compare the fractions by writing >, <, or = on the lines.

i.
$$\frac{7}{12}$$
 $\frac{1}{2}$

ii.
$$\frac{7}{12}$$
 $\frac{5}{6}$

- 2. a. Plot the following points on the number line without measuring.





b. Select two fractions from Part (a), and use the given number line to compare them by writing >, <, or =.

c. Explain how you plotted the points in Part (a).

- 3. Compare the fractions given below by writing > or < on the lines. Give a brief explanation for each answer referring to the benchmarks 0, $\frac{1}{2}$, and 1.
 - a. $\frac{1}{2}$ $\frac{3}{4}$

b. $\frac{1}{2}$ $\frac{7}{8}$

c. $\frac{2}{3}$ $\frac{2}{5}$

 $d_{10} = \frac{9}{10} = \frac{3}{5}$

e. $\frac{2}{3}$ $\frac{7}{8}$

 f_{*} $\frac{1}{3}$ $\frac{2}{4}$

g. $\frac{2}{3}$ $\frac{5}{10}$

 $h_{*} = \frac{11}{12} = \frac{2}{5}$

i. $\frac{49}{100}$ $\frac{51}{100}$

j. $\frac{7}{16}$ $\frac{51}{100}$

- 1. Plot the following points on the number line without measuring.
 - a. $\frac{8}{10}$

c. $\frac{1}{4}$



1	
_	
2	
Ĭ.	

1	
1	_
	$\overline{}$

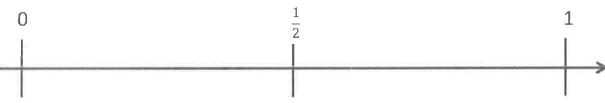
- 2. Use the number line in Problem 1 to compare the fractions by writing >, <, or = on the lines.
 - a. $\frac{1}{4}$ $\frac{1}{2}$
 - b. $\frac{8}{10}$ $\frac{3}{5}$
 - $c_{*} = \frac{1}{2}$
 - d. $\frac{1}{4}$ $\frac{8}{10}$

1

Application Problem

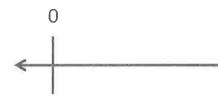




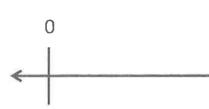




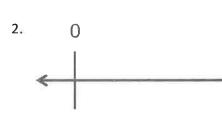














number line



		s.			
			W		

Mr. and Mrs. Reynolds went for a run. Mr. Reynolds ran for $\frac{6}{10}$ mile. Mrs. Reynolds ran for $\frac{2}{5}$ mile. Who ran farther? Explain how you know. Use the benchmarks 0, $\frac{1}{2}$, and 1 to explain your answer.

.

Reason using benchmarks to compare two fractions on the

Draw

Write

Lesson 13:

Read

		*		

- 1. Place the following fractions on the number line given.
 - a. $\frac{4}{3}$

 b_{\bullet} $\frac{11}{6}$

c. $\frac{17}{12}$

1

1	<u>1</u> 2	
-	_	

2	
	_

- 2. Use the number line in Problem 1 to compare the fractions by writing >, <, or = on the lines.

 - a. $1\frac{5}{6}$ b. $1\frac{1}{3}$ b. $1\frac{1}{3}$
- 3. Place the following fractions on the number line given.
 - a. $\frac{11}{8}$





4. Use the number line in Problem 3 to explain the reasoning you used when determining whether $\frac{11}{8}$ or $\frac{15}{12}$ is greater.

5. Compare the fractions given below by writing > or < on the lines. Give a brief explanation for each answer referring to benchmarks.

$$a_{*} = \frac{3}{8} = \frac{7}{12}$$

b.
$$\frac{5}{12}$$
 $\frac{7}{8}$

c.
$$\frac{8}{6}$$
 $\frac{11}{12}$

d.
$$\frac{5}{12}$$
 $\frac{1}{3}$

e.
$$\frac{7}{5}$$
 $\frac{11}{10}$

f.
$$\frac{5}{4}$$
 $\frac{7}{8}$

g.
$$\frac{13}{12}$$
 $\frac{9}{10}$

h.
$$\frac{6}{8}$$
 $\frac{5}{4}$

i.
$$\frac{8}{12}$$
 $\frac{8}{4}$

j.
$$\frac{7}{5}$$
 $\frac{16}{10}$

- 1. Place the following fractions on the number line given.
 - a. $\frac{5}{4}$

b. $\frac{10}{7}$

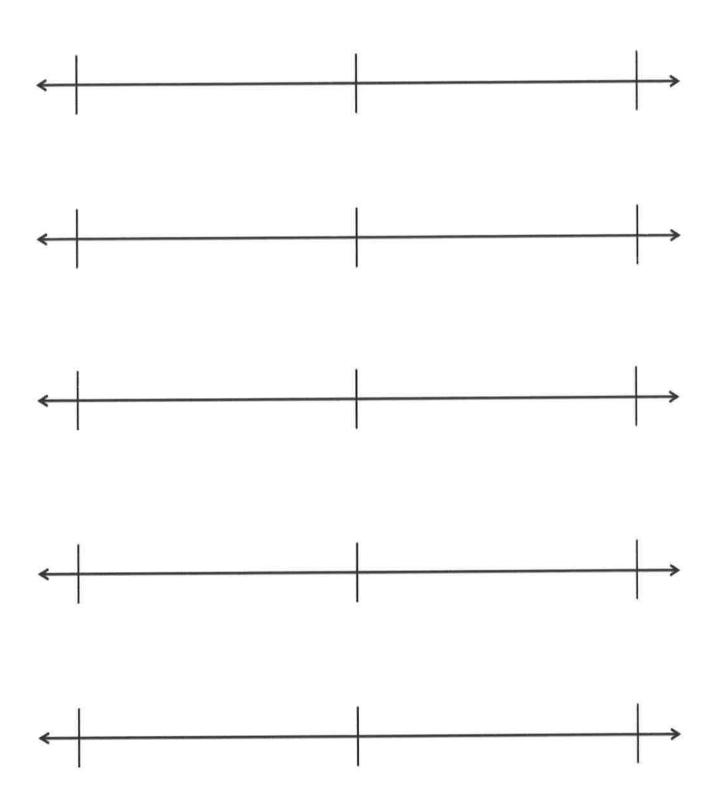
c. $\frac{16}{9}$



- 2. Compare the fractions using >, <, or =.

- a. $\frac{5}{4}$ b. $\frac{5}{4}$ c. $\frac{16}{9}$ c. $\frac{16}{9}$

	19		
15			



blank number lines with midpoint



				*

Compare $\frac{4}{5}, \frac{3}{4}$, and $\frac{9}{10}$ using <, >, or =. Explain your reasoning using a benchmark.

Read

Draw

Write



Lesson 14:

Find common units or number of units to compare two fractions.

Name	Date	

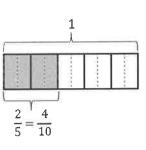
- 1. Compare the pairs of fractions by reasoning about the size of the units. Use >, <, or =.
 - a. 1 fourth _____ 1 fifth

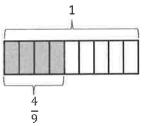
b. 3 fourths _____ 3 fifths

c. 1 tenth _____ 1 twelfth

- d. 7 tenths _____ 7 twelfths
- 2. Compare by reasoning about the following pairs of fractions with the same or related numerators. Use >, <, or =. Explain your thinking using words, pictures, or numbers. Problem 2(b) has been done for you.
 - a. $\frac{3}{5}$ $\frac{3}{4}$

b. $\frac{2}{5} < \frac{4}{9}$ because $\frac{2}{5} = \frac{4}{10}$ 4 tenths is less than 4 ninths because tenths are smaller than ninths.





c. $\frac{7}{11}$ $\frac{7}{13}$

d. $\frac{6}{7}$ $\frac{12}{15}$



3. Draw two tape diagrams to model each pair of the following fractions with related denominators. Use >, <, or = to compare.

a.
$$\frac{2}{3} - \frac{5}{6}$$

b.
$$\frac{3}{4} - \frac{7}{8}$$

c.
$$1\frac{3}{4}$$
 _____1

4. Draw one number line to model each pair of fractions with related denominators. Use >, <, or = to compare.

a.
$$\frac{2}{3}$$
 $\frac{5}{6}$

b.
$$\frac{3}{8}$$
 $\frac{1}{4}$

c.
$$\frac{2}{6}$$
 $\frac{5}{12}$

d.
$$\frac{8}{9}$$
 $\frac{2}{3}$

5. Compare each pair of fractions using >, <, or =. Draw a model if you choose to.

a.
$$\frac{3}{4}$$
 $\frac{3}{7}$

b.
$$\frac{4}{5}$$
 $\frac{8}{12}$

c.
$$\frac{7}{10}$$
 $\frac{3}{5}$

d.
$$\frac{2}{3}$$
 $\frac{11}{15}$

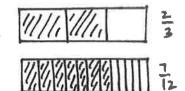
e.
$$\frac{3}{4} = \frac{11}{12}$$

f.
$$\frac{7}{3}$$
 $\frac{7}{4}$

g.
$$1\frac{1}{3}$$
 $1\frac{2}{9}$

h.
$$1\frac{2}{3}$$
 $1\frac{4}{7}$

6. Timmy drew the picture to the right and claimed that $\frac{2}{3}$ is less than $\frac{7}{12}$. Evan says he thinks $\frac{2}{3}$ is greater than $\frac{7}{12}$. Who is correct? Support your answer with a picture.



Name	Date
Turile	

1. Draw tape diagrams to compare the following fractions:

2. Use a number line to compare the following fractions:



Jamal ran $\frac{2}{3}$ mile. Ming ran $\frac{2}{4}$ mile. Laina ran $\frac{7}{12}$ mile. Who ran the farthest? What do you think is the easiest way to determine the answer to this question?

Read

Draw

Write



Lesson 15:

Find common units or number of units to compare two fractions.

Name	Date
ivairie	

1. Draw an area model for each pair of fractions, and use it to compare the two fractions by writing >, <, or = on the line. The first two have been partially done for you. Each rectangle represents 1.

a.	<u>1</u>	<	$-\frac{2}{3}$	~~~		
			$\frac{1\times3}{2\times3} = \frac{3}{6}$		 	

$$\frac{2\times2}{3\times2} = \frac{4}{6}$$

h.	4	3
D,	5	4

 _	 	

		_	

	3	4
U.	_	
	5	7

٦.	3	2
a.	- 7	

A	5	6
· ·		
	8	- 9

f.
$$\frac{2}{3}$$
 $\frac{3}{4}$



2. Rename the fractions, as needed, using multiplication in order to compare each pair of fractions by writing >, <, or =.

a.
$$\frac{3}{5}$$
 $\frac{5}{6}$

b.
$$\frac{2}{6}$$
 $\frac{3}{8}$

c.
$$\frac{7}{5}$$
 $\frac{10}{8}$

d.
$$\frac{4}{3}$$
 $\frac{6}{5}$

3. Use any method to compare the fractions. Record your answer using >, <, or =.

a.
$$\frac{3}{4}$$
 $\frac{7}{8}$

b.
$$\frac{6}{8}$$
 $\frac{3}{5}$

c.
$$\frac{6}{4}$$
 $\frac{8}{6}$

d.
$$\frac{8}{5}$$
 $\frac{9}{6}$

© 2018 Great Minds*. eureka-math.org

4. Explain two ways you have learned to compare fractions. Provide evidence using words, pictures, or numbers.



ž.			
		N	

Name	Date
Marrie	100000000000000000000000000000000000000

Draw an area model for each pair of fractions, and use it to compare the two fractions by writing >, <, or = on the line.

1.
$$\frac{3}{4}$$
 $\frac{4}{5}$

2.
$$\frac{2}{6}$$
 $\frac{3}{5}$



				4.

Keisha ran $\frac{5}{6}$ mile in the morning and $\frac{2}{3}$ mile in the afternoon.	Did Keisha run farther in the morning
or in the afternoon? Explain.	

Lesson 16:

Use visual models to add and subtract two fractions with the same units.

Draw

Write

113



Read

	::		

Name _____

1. Solve.

- a. 3 fifths 1 fifth = _____
- b. 5 fifths 3 fifths = _____
- c. 3 halves 2 halves = _____
- d. 6 fourths 3 fourths = _____

2. Solve.

a. $\frac{5}{6} - \frac{3}{6}$

b. $\frac{6}{8} - \frac{4}{8}$

c. $\frac{3}{10} - \frac{3}{10}$

d. $\frac{5}{5} - \frac{4}{5}$

e. $\frac{5}{4} - \frac{4}{4}$

f. $\frac{5}{4} - \frac{3}{4}$

3. Solve. Use a number bond to show how to convert the difference to a mixed number. Problem (a) has been completed for you.

a. $\frac{12}{8} - \frac{3}{8} = \frac{9}{8} = 1\frac{1}{8}$



d. $\frac{14}{8} - \frac{3}{8}$

e. $\frac{8}{4} - \frac{2}{4}$

c. $\frac{9}{5} - \frac{3}{5}$

f. $\frac{15}{10} - \frac{3}{10}$

- 4. Solve. Write the sum in unit form.
 - a. 2 fourths + 1 fourth = _____
- b. 4 fifths + 3 fifths = _____

5. Solve.

$$a_{*} = \frac{2}{8} + \frac{5}{8}$$

b.
$$\frac{4}{12} + \frac{5}{12}$$

6. Solve. Use a number bond to decompose the sum. Record your final answer as a mixed number. Problem (a) has been completed for you.

a.
$$\frac{3}{5} + \frac{4}{5} = \frac{7}{5} = 1\frac{2}{5}$$

$$\frac{5}{5} = \frac{2}{5}$$

$$b = \frac{4}{4} + \frac{3}{4}$$

c.
$$\frac{6}{9} + \frac{6}{9}$$

$$d = \frac{7}{10} + \frac{6}{10}$$

e.
$$\frac{5}{6} + \frac{7}{6}$$

$$f_{1} = \frac{9}{8} + \frac{5}{8}$$

7. Solve. Use a number line to model your answer.

a.
$$\frac{7}{4} - \frac{5}{4}$$

b.
$$\frac{5}{4} + \frac{2}{4}$$

Date _____

1. Solve. Use a number bond to decompose the difference. Record your final answer as a mixed number.

$$\frac{16}{9} - \frac{5}{9}$$

2. Solve. Use a number bond to decompose the sum. Record your final answer as a mixed number.

$$\frac{5}{12} + \frac{10}{12}$$

			2
	9.		

Name_		Date
		→
	-	→
	-	
	<	
	\	

blank number lines



Lesson 16:

Use visual models to add and subtract two fractions with the same

Use a number bond to show the relationship between $\frac{2}{3}$, $\frac{3}{6}$, and $\frac{5}{6}$. Then, use the fractions to write two addition and two subtraction sentences.

Read

Draw

Write



Lesson 17:

Use visual models to add and subtract two fractions with the same units, including subtracting from one whole.

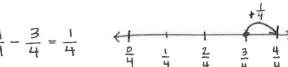
				*	

Date ____

1. Use the following three fractions to write two subtraction and two addition number sentences.

2. Solve. Model each subtraction problem with a number line, and solve by both counting up and subtracting. Part (a) has been completed for you.

a. $1 - \frac{3}{4}$



c. $1 - \frac{3}{5}$

b. $1 - \frac{8}{10}$

d. $1 - \frac{5}{8}$

e. $1\frac{2}{10} - \frac{7}{10}$

 $f_0 = 1\frac{1}{5} - \frac{3}{5}$

3. Find the difference in two ways. Use number bonds to decompose the total. Part (a) has been completed for you.

a.
$$1\frac{2}{5} - \frac{4}{5}$$
 $\frac{5}{5}$
 $\frac{2}{5}$

$$\frac{5}{5} + \frac{2}{5} = \frac{7}{5}$$

$$\frac{7}{5} - \frac{4}{5} = \frac{3}{5}$$

$$\frac{7}{5} - \frac{4}{5} = \left(\frac{3}{5}\right)$$

$$\frac{5}{5} - \frac{4}{5} = \frac{1}{5}$$

$$\frac{1}{5} + \frac{2}{5} = \left(\frac{3}{5}\right)$$

b.
$$1\frac{3}{6} - \frac{4}{6}$$

c.
$$1\frac{6}{8} - \frac{7}{8}$$

d.
$$1\frac{1}{10} - \frac{7}{10}$$

e.
$$1\frac{3}{12} - \frac{6}{12}$$

1. Solve. Model the problem with a number line, and solve by both counting up and subtracting.

$$1-\frac{2}{5}$$

2. Find the difference in two ways. Use a number bond to show the decomposition.

$$1\frac{2}{7} - \frac{5}{7}$$

*		
(a)		

ame		Date
Problem A:	$\frac{1}{8} + \frac{3}{8} + \frac{4}{8}$	
Problem B:	$\frac{1}{6} + \frac{4}{6} + \frac{2}{6}$	
Problem C:	$\frac{11}{10} - \frac{4}{10} - \frac{1}{10}$	

adding and subtracting fractions



Problem D:	$1 - \frac{3}{12} - \frac{5}{12}$	
Problem E:	$\frac{5}{8} + \frac{4}{8} + \frac{1}{8}$	
Problem F:	$1\frac{1}{5} - \frac{2}{5} - \frac{3}{5}$	Resease Andrew Control of the Contro

adding and subtracting fractions



Date _____ Name _____

Show one way to solve each problem. Express sums and differences as a mixed number when possible. Use number bonds when it helps you. Part (a) is partially completed.

a.	$\frac{2}{5} + \frac{3}{5} + \frac{1}{5}$	
	$= \frac{5}{5} + \frac{1}{5} = 1 +$	$\frac{1}{5}$
	=	

b.
$$\frac{3}{6} + \frac{1}{6} + \frac{3}{6}$$

c.
$$\frac{5}{7} + \frac{7}{7} + \frac{2}{7}$$

d.
$$\frac{7}{8} - \frac{3}{8} - \frac{1}{8}$$

e.
$$\frac{7}{9} + \frac{1}{9} + \frac{4}{9}$$

$$f_* \quad \frac{4}{10} + \frac{11}{10} + \frac{5}{10}$$

g.
$$1 - \frac{3}{12} - \frac{4}{12}$$

h.
$$1\frac{2}{3} - \frac{1}{3} - \frac{1}{3}$$

i.
$$\frac{10}{12} + \frac{5}{12} + \frac{2}{12} + \frac{7}{12}$$

*

2. Monica and Stuart used different strategies to solve $\frac{5}{8} + \frac{2}{8} + \frac{5}{8}$.

Monica's Way

$$\frac{5}{8} + \frac{2}{8} + \frac{5}{8} = \frac{7}{8} + \frac{5}{8} = \frac{8}{8} + \frac{4}{8} = 1\frac{4}{8}$$

$$\frac{1}{8} \quad \frac{4}{8}$$

Stuart's Way

$$\frac{5}{8} + \frac{2}{8} + \frac{5}{8} = \frac{12}{8} = 1 + \frac{4}{8} = 1\frac{4}{8}$$

$$\frac{8}{8} \quad \frac{4}{8}$$

Whose strategy do you like best? Why?

3. You gave one solution for each part of Problem 1. Now, for each problem indicated below, give a different solution method.

1(c)
$$\frac{5}{7} + \frac{7}{7} + \frac{2}{7}$$

1(f)
$$\frac{4}{10} + \frac{11}{10} + \frac{5}{10}$$

1(g)
$$1 - \frac{3}{12} - \frac{4}{12}$$

Solve the following problems. Use number bonds to help you.

1.
$$\frac{5}{9} + \frac{2}{9} + \frac{4}{9}$$

2.
$$1-\frac{5}{8}-\frac{1}{8}$$

Fractions are all around us! Make a list of times that you have used fractions, heard fractions, or seen fractions. Be ready to share your ideas.					



Lesson 19:

Solve word problems involving addition and subtraction of fractions,

Draw

Write

Read

Name	Date	
Name	Bute	

Use the RDW process to solve.

1. Sue ran $\frac{9}{10}$ mile on Monday and $\frac{7}{10}$ mile on Tuesday. How many miles did Sue run in the 2 days?

2. Mr. Salazar cut his son's birthday cake into 8 equal pieces. Mr. Salazar, Mrs. Salazar, and the birthday boy each ate 1 piece of cake. What fraction of the cake was left?

3. Maria spent $\frac{4}{7}$ of her money on a book and saved the rest. What fraction of her money did Maria save?



4. Mrs. Jones had $1\frac{4}{8}$ pizzas left after a party. After giving some to Gary, she had $\frac{7}{8}$ pizza left. What fraction of a pizza did she give Gary?

5. A baker had 2 pans of corn bread. He served $1\frac{1}{4}$ pans. What fraction of a pan was left?

6. Marius combined $\frac{4}{8}$ gallon of lemonade, $\frac{3}{8}$ gallon of cranberry juice, and $\frac{6}{8}$ gallon of soda water to make punch for a party. How many gallons of punch did he make in all?



Name	Date
Ivaille	

Use the RDW process to solve.

1. Mrs. Smith took her bird to the vet. Tweety weighed $1\frac{3}{10}$ pounds. The vet said that Tweety weighed $\frac{4}{10}$ pound more last year. How much did Tweety weigh last year?

2. Hudson picked $1\frac{1}{4}$ baskets of apples. Suzy picked 2 baskets of apples. How many more baskets of apples did Suzy pick than Hudson?



	¥	

Krista drank $\frac{3}{16}$ of the water in her water bottle in the morning, $\frac{5}{16}$ in the afternoon, and $\frac{3}{16}$ in the evening. What fraction of water was left at the end of the day?

Read

Draw

Write



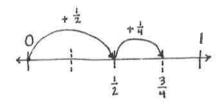
Lesson 20:

2. Estimate to determine if the sum is between 0 and 1 or 1 and 2. Draw a number line to model the addition. Then, write a complete number sentence. Part (a) has been completed for you.



a.
$$\frac{1}{2} + \frac{1}{4}$$
 $\frac{2}{4} + \frac{1}{4} = \frac{3}{4}$

b.
$$\frac{1}{2} + \frac{4}{10}$$



c.
$$\frac{6}{10} + \frac{1}{2}$$

d.
$$\frac{2}{3} + \frac{3}{6}$$

e.
$$\frac{3}{4} + \frac{6}{8}$$

f.
$$\frac{4}{10} + \frac{6}{5}$$

3. Solve the following addition problem without drawing a model. Show your work.

$$\frac{2}{3} + \frac{4}{6}$$

1. Draw a number line to model the addition. Solve, and then write a complete number sentence.

$$\frac{5}{8} + \frac{2}{4}$$

2. Solve without drawing a model.

$$\frac{3}{4} + \frac{1}{2}$$



Two-fifths liter of chemical A was added to $\frac{7}{10}$ liter of chemical B to make chemical C. How many liters of chemical C are there?

Read

Draw

Write



Lesson 21:

Use visual models to add two fractions with related units using the denominators 2, 3, 4, 5, 6, 8, 10, and 12.

<u>ģ</u> i			

- Draw a tape diagram to represent each addend. Decompose one of the tape diagrams to make like units. Then, write a complete number sentence. Use a number bond to write each sum as a mixed number.
 - a. $\frac{3}{4} + \frac{1}{2}$

 $b_{1} = \frac{2}{3} + \frac{3}{6}$

c. $\frac{5}{6} + \frac{1}{3}$

 $d_{\star} = \frac{4}{5} + \frac{7}{10}$

- 2. Draw a number line to model the addition. Then, write a complete number sentence. Use a number bond to write each sum as a mixed number.
 - a. $\frac{1}{2} + \frac{3}{4}$

 $b_1 = \frac{1}{2} + \frac{6}{8}$

$$c_{10} = \frac{7}{10} + \frac{3}{5}$$

$$d_{1/2} \frac{2}{3} + \frac{5}{6}$$

3. Solve. Write the sum as a mixed number. Draw a model if needed.

$$a_* = \frac{3}{4} + \frac{2}{8}$$

$$b_{\bullet} = \frac{4}{6} + \frac{1}{2}$$

$$c_{11} = \frac{4}{6} + \frac{2}{3}$$

d.
$$\frac{8}{10} + \frac{3}{5}$$

e.
$$\frac{5}{8} + \frac{3}{4}$$

$$f_{\odot}$$
 $\frac{5}{8} + \frac{2}{4}$

g.
$$\frac{1}{2} + \frac{5}{8}$$

h.
$$\frac{3}{10} + \frac{4}{5}$$

Name	Date

Solve. Write a complete number sentence. Use a number bond to write each sum as a mixed number. Use a model if needed.

1.
$$\frac{1}{4} + \frac{7}{8}$$

2.
$$\frac{2}{3} + \frac{7}{12}$$



Winnie went shopping and spent $\frac{2}{5}$ of the money that was on a gift card. What fraction of the money was left on the card? Draw a number line and a number bond to help show your thinking.

Read

Draw

Write



Lesson 22:

Add a fraction less than 1 to, or subtract a fraction less than 1 from, a whole number using decomposition and visual models.

9		

1. Draw a tape diagram to match each number sentence. Then, complete the number sentence.

a.
$$3 + \frac{1}{2} =$$

b.
$$4 + \frac{3}{4} =$$

c.
$$3 - \frac{1}{4} =$$

d.
$$5 - \frac{2}{5} =$$

2. Use the following three numbers to write two subtraction and two addition number sentences.

a. 6,
$$6\frac{3}{8}$$
, $\frac{3}{8}$

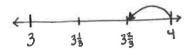
b.
$$\frac{4}{7}$$
, 9, $8\frac{3}{7}$

3. Solve using a number bond. Draw a number line to represent each number sentence. The first one has been done for you.

a.
$$4 - \frac{1}{3} = 3\frac{2}{3}$$

b.
$$5 - \frac{2}{3} =$$

$$4 - \frac{1}{3} = 3\frac{2}{3}$$



c.
$$7 - \frac{3}{8} =$$

d.
$$10 - \frac{4}{10} =$$

4. Complete the subtraction sentences using number bonds.

a.
$$3 - \frac{1}{10} =$$

b.
$$5 - \frac{3}{4} =$$

c.
$$6 - \frac{5}{8} =$$

d.
$$7 - \frac{3}{9} =$$

e.
$$8 - \frac{6}{10} =$$

f.
$$29 - \frac{9}{12} =$$

Date _____

Complete the subtraction sentences using number bonds. Draw a model if needed.

1.
$$6 - \frac{1}{5} =$$

2.
$$8 - \frac{5}{6} =$$

3.
$$7 - \frac{5}{8} =$$

×.		

Mrs. Wilcox cut quilt squares and then divided them evenly into 8 piles. She decided to sew together 1 pile each night. After 5 nights, what fraction of the quilt squares was sewn together? Draw a tape diagram or a number line to model your thinking, and then write a number sentence to express your answer.

Read **Draw** Write

Add and multiply unit fractions to build fractions greater than 1 using

Lesson 23:

			.1

Name	Date

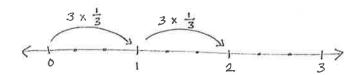
- 1. Circle any fractions that are equivalent to a whole number. Record the whole number below the fraction.
 - a. Count by 1 thirds. Start at 0 thirds. End at 6 thirds.

$$\frac{0}{3}, \frac{1}{3},$$

- b. Count by 1 halves. Start at 0 halves. End at 8 halves.
- 2. Use parentheses to show how to make ones in the following number sentence.

$$\frac{1}{4} + \frac{1}{4} = 3$$

- 3. Multiply, as shown below. Draw a number line to support your answer.
 - a. $6 \times \frac{1}{3}$

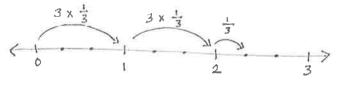


$$6 \times \frac{1}{3} = 2 \times \frac{3}{3} = 2$$

b. $6 \times \frac{1}{2}$

c. $12 \times \frac{1}{4}$

- 4. Multiply, as shown below. Write the product as a mixed number. Draw a number line to support your answer.
 - a. 7 copies of 1 third



$$7 \times \frac{1}{3} = (2 \times \frac{3}{3}) + \frac{1}{3} = 2 + \frac{1}{3} = 2\frac{1}{3}$$

b. 7 copies of 1 half

c.
$$10 \times \frac{1}{4}$$

d.
$$14 \times \frac{1}{3}$$

Multiply and write the product as a mixed number. Draw a number line to support your answer.

1. $8 \times \frac{1}{2}$

2. 7 copies of 1 fourth

3. $13 \times \frac{1}{3}$



В			

Shelly read her book for $\frac{1}{2}$ hour each afternoon for 9 days. How many hours did Shelly spend reading in all 9 days?

Read

Draw

Write



Lesson 24:

Decompose and compose fractions greater than 1 to express them in various forms.

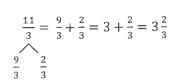
		5

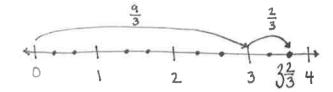
Name _____

Date _____

1. Rename each fraction as a mixed number by decomposing it into two parts as shown below. Model the decomposition with a number line and a number bond.





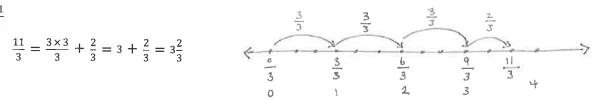


 $b_{*} = \frac{12}{5}$

c. $\frac{13}{2}$

d. $\frac{15}{4}$

 $a_{*} \frac{11}{3}$



- **b.** $\frac{9}{2}$

3. Convert each fraction to a mixed number.

a. $\frac{9}{4}$ =	b. $\frac{17}{5} =$	c. $\frac{25}{6}$ =
d. $\frac{30}{7} =$	e. $\frac{38}{8}$ =	f. $\frac{48}{9}$ =
g. $\frac{63}{10} =$	$h_{\bullet} = \frac{84}{10} =$	i. $\frac{37}{12}$ =

Name	Date
idilic	Date

1. Rename the fraction as a mixed number by decomposing it into two parts. Model the decomposition with a number line and a number bond.

2. Convert the fraction to a mixed number. Model with a number line.

 $\frac{19}{3}$

3. Convert the fraction to a mixed number.

11 4

Mrs. Fowler knew that the perimeter of the soccer field was $\frac{1}{6}$ mile. Her goal was to walk two miles while watching her daughter's game. If she walked around the field 13 times, did she meet her goal? Explain your thinking.

Read

Draw

Write

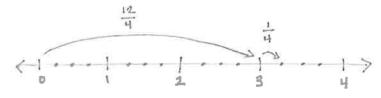


Lesson 25:

Decompose and compose fractions greater than 1 to express them in

Name	Date
1101110	110043700-

- 1. Convert each mixed number to a fraction greater than 1. Draw a number line to model your work.
 - a. $3\frac{1}{4}$



$$3\frac{1}{4} = 3 + \frac{1}{4} = \frac{12}{4} + \frac{1}{4} = \frac{13}{4}$$

b. $2\frac{4}{5}$

c. $3\frac{5}{8}$

d. $4\frac{4}{10}$

e. $4\frac{7}{9}$

- 2. Convert each mixed number to a fraction greater than 1. Show your work as in the example. (Note: $3 \times \frac{4}{4} = \frac{3 \times 4}{4}$.)
 - a. $3\frac{3}{4}$

$$3\frac{3}{4} = 3 + \frac{3}{4} = \left(3 \times \frac{4}{4}\right) + \frac{3}{4} = \frac{12}{4} + \frac{3}{4} = \frac{15}{4}$$

- b. $4\frac{1}{3}$
- c. $4\frac{3}{5}$
- d. $4\frac{6}{8}$
- 3. Convert each mixed number to a fraction greater than 1.

a. $2\frac{3}{4}$	b. $2\frac{2}{5}$	c. $3\frac{3}{6}$
d. $3\frac{3}{8}$	e. $3\frac{1}{10}$	f_{*} $4\frac{3}{8}$
$g. 5\frac{2}{3}$	h. $6\frac{1}{2}$	i. $7\frac{3}{10}$

Convert each mixed number to a fraction greater than 1.

1. $3\frac{1}{5}$

2. $2\frac{3}{5}$

3. $4\frac{2}{9}$



		29/1		

Barbara needed $3\frac{1}{4}$ cups of flour for her recipe.	If she measured $\frac{1}{4}$ cup at a time, how many times
did she have to fill the measuring cup?	

Read

Draw

Write



Lesson 26:

					3
				a a	

- 1. a. Plot the following points on the number line without measuring.
 - i. $2\frac{7}{8}$

ii. $3\frac{1}{6}$

iii. $\frac{29}{12}$



3



- b. Use the number line in Problem 1(a) to compare the fractions by writing >, <, or =.
 - i. $\frac{29}{12}$ $2\frac{7}{8}$

- ii. $\frac{29}{12}$ _____3 $\frac{1}{6}$
- 2. a. Plot the following points on the number line without measuring.

ii. $8\frac{2}{4}$

iii. $\frac{25}{3}$





- b. Compare the following by writing >, <, or =.
 - i. $8\frac{2}{4}$ $\frac{25}{3}$

- ii. $\frac{70}{9}$ 8 $\frac{2}{4}$
- Explain how you plotted the points in Problem 2(a).

3. Compare the fractions given below by writing >, <, or =. Give a brief explanation for each answer, referring to benchmark fractions.

a.
$$5\frac{1}{3}$$
 4 $\frac{3}{4}$

b.
$$\frac{12}{6}$$
 $\frac{25}{12}$

$$c. \frac{18}{7} = \frac{17}{5}$$

d.
$$5\frac{2}{5}$$
_5

e.
$$6\frac{2}{3}$$
 ______6 $\frac{3}{7}$

$$f_{\bullet} = \frac{31}{7} = \frac{32}{8}$$

g.
$$\frac{31}{10}$$
 $\frac{25}{8}$

h.
$$\frac{39}{12}$$
 $\frac{19}{6}$

i.
$$\frac{49}{50}$$
 ______3 $\frac{90}{100}$

j.
$$5\frac{5}{12}$$
 $5\frac{51}{100}$

Date _____

Compare the fractions given below by writing >, <, or =.

Give a brief explanation for each answer, referring to benchmark fractions.

1.
$$3\frac{2}{3}$$
 ______3 $\frac{4}{6}$

2.
$$\frac{12}{3}$$
 $\frac{27}{7}$

3.
$$\frac{10}{6}$$
 $\frac{5}{4}$

4.
$$3\frac{2}{5}$$
 $3\frac{3}{10}$



			,		
-1					

Jeremy ran 27 laps on a track that was $\frac{1}{8}$ mile long.	Jimmy ran 15 laps on a track that was	$\frac{1}{4}$ mile long.
Who ran farther?		

Read

Draw

Write



я		

Date _____

- 1. Draw a tape diagram to model each comparison. Use >, <, or = to compare.
 - a. $3\frac{2}{3}$ ______ $3\frac{5}{6}$

b. $3\frac{2}{5}$ _____3 $\frac{6}{10}$

c. $4\frac{3}{6}$ _____ $4\frac{1}{3}$

d. $4\frac{5}{8}$ $\frac{19}{4}$

- 2. Use an area model to make like units. Then, use >, <, or = to compare.
 - a. $2\frac{3}{5}$ $\frac{18}{7}$

b. $2\frac{3}{8}$ $2\frac{1}{3}$

3. Compare each pair of fractions using >, <, or = using any strategy.

a.
$$5\frac{3}{4}$$
____5 $\frac{3}{8}$

b.
$$5\frac{2}{5}$$
_____ $5\frac{8}{10}$

c.
$$5\frac{6}{10}$$
 $\frac{27}{5}$

d.
$$5\frac{2}{3}$$
_____ $5\frac{9}{15}$

e.
$$\frac{7}{2}$$
 $\frac{7}{3}$

f.
$$\frac{12}{3}$$
 $\frac{15}{4}$

g.
$$\frac{22}{5}$$
 _____4 $\frac{2}{7}$

h.
$$\frac{21}{4}$$
____5

i.
$$\frac{29}{8}$$
 _______ $\frac{11}{3}$

$$j$$
. $3\frac{3}{4}$ _______3 $\frac{4}{7}$

Compare each pair of fractions using >, <, or = using any strategy.

1.
$$4\frac{3}{8}$$
 $4\frac{1}{4}$

2.
$$3\frac{4}{5}$$
 3 $\frac{9}{10}$

3.
$$2\frac{1}{3}$$
 $2\frac{2}{5}$

4.
$$10\frac{2}{5}$$
 _____ $10\frac{3}{4}$



Name	Date
Nullic	

1. The chart to the right shows the distance fourth graders in Ms. Smith's class were able to run before stopping for a rest. Create a line plot to display the data in the table.

Student	Distance (in miles)
Joe	$2\frac{1}{2}$
Arianna	$1\frac{3}{4}$
Bobbi	$2\frac{1}{8}$
Morgan	1 = 1
Jack	2 5/8
Saisha	$2\frac{1}{4}$
Tyler	$2\frac{2}{4}$
Jenny	$\frac{5}{8}$
Anson	$2\frac{2}{8}$
Chandra	24/8



- 2. Solve each problem.
 - a. Who ran a mile farther than Jenny?
 - b. Who ran a mile less than Jack?
 - c. Two students ran exactly $2\frac{1}{4}$ miles. Identify the students. How many quarter miles did each student run?
 - d. What is the difference, in miles, between the longest and shortest distance run?
 - e. Compare the distances run by Arianna and Morgan using >, <, or =.
 - f. Ms. Smith ran twice as far as Jenny. How far did Ms. Smith run? Write her distance as a mixed number.
 - g. Mr. Reynolds ran $1\frac{3}{10}$ miles. Use >, <, or = to compare the distance Mr. Reynolds ran to the distance that Ms. Smith ran. Who ran farther?
- 3. Using the information in the table and on the line plot, develop and write a question similar to those above. Solve, and then ask your partner to solve. Did you solve in the same way? Did you get the same answer?

Nama a	Date
Name	Date

Mr. O'Neil asked his students to record the length of time they read over the weekend. The times are listed in the table.

1. At the bottom of the page, make a line plot of the data.

2. One of the students read $\frac{3}{4}$ hour on Friday, $\frac{3}{4}$ hour on Saturday, and $\frac{3}{4}$ hour on Sunday. How many hours did that student read over the weekend? Name that student.

Student	Length of time (in hours)
Robin	1/2
Bill	1
Katrina	3 4
Kelly	1 3 4
Mary	$1\frac{1}{2}$
Gail	$2\frac{1}{4}$
Scott	1 3 4
Ben	22/4



Both Allison and Jennifer jogged on Sunday. When asked about their distances, Allison said, "I ran $2\frac{7}{8}$ miles this morning and $3\frac{3}{8}$ miles this afternoon. So, I ran a total of about 6 miles," and Jennifer said, "I ran $3\frac{1}{10}$ miles this morning and $3\frac{3}{10}$ miles this evening. I ran a total of $6\frac{4}{10}$ miles." How do their answers differ?

Draw

Write

Estimate sums and differences using benchmark numbers.

Read

Date _____

1. Estimate each sum or difference to the nearest half or whole number by rounding. Explain your estimate using words or a number line.

a.
$$2\frac{1}{12} + 1\frac{7}{8} \approx$$

b.
$$1\frac{11}{12} + 5\frac{3}{4} \approx$$

c.
$$8\frac{7}{8} - 2\frac{1}{9} \approx$$

d.
$$6\frac{1}{8} - 2\frac{1}{12} \approx$$

e.
$$3\frac{3}{8} + 5\frac{1}{9} \approx$$

2. Estimate each sum or difference to the nearest half or whole number by rounding. Explain your estimate using words or a number line.

$$a_{10} = \frac{16}{5} + \frac{11}{4} \approx \underline{\hspace{1cm}}$$

b.
$$\frac{17}{3} - \frac{15}{7} \approx$$

C.
$$\frac{59}{10} + \frac{26}{10} \approx$$

3. Montoya's estimate for $8\frac{5}{8} - 2\frac{1}{3}$ was 7. Julio's estimate was $6\frac{1}{2}$. Whose estimate do you think is closer to the actual difference? Explain.

4. Use benchmark numbers or mental math to estimate the sum or difference.

a. $14\frac{3}{4} + 29\frac{11}{12}$	b. $3\frac{5}{12} + 54\frac{5}{8}$
c. $17\frac{4}{5} - 8\frac{7}{12}$	d. $\frac{65}{8} - \frac{37}{6}$

© 2018 Great Minds®, eureka-math.org

Estimate each sum or difference to the nearest half or whole number by rounding. Explain your estimate using words or a number line.

1.
$$2\frac{9}{10} + 2\frac{1}{4} \approx$$

2.
$$11\frac{8}{9} - 3\frac{3}{8} \approx$$

One board measures 2 meters 70 centimeters. Another measures 87 centimeters. What is the total length of the two boards expressed in meters and centimeters?	
	-
	-



Lesson 30:

Add a mixed number and a fraction.

Draw

Write

Read

Name _____

1. Solve.

$$3\frac{1}{4} + \frac{1}{4}$$

b.
$$7\frac{3}{4} + \frac{1}{4}$$

C.
$$\frac{3}{8} + 5\frac{2}{8}$$

$$d_* = \frac{1}{8} + 6\frac{7}{8}$$

2. Complete the number sentences.

a.	$4\frac{7}{8} + $	= 5
۳.	' ₈ '—	

$$7\frac{2}{5} + \underline{\hspace{1cm}} = 8$$

d.

c.
$$3 = 2\frac{1}{6} + \frac{1}{6}$$

$$12 = 11\frac{1}{12} +$$

3. Use a number bond and the arrow way to show how to make one. Solve.

a.
$$2\frac{3}{4} + \frac{2}{4}$$

b.
$$3\frac{3}{5} + \frac{3}{5}$$



4. Solve.

a. $4\frac{2}{3} + \frac{2}{3}$	b. $3\frac{3}{5} + \frac{4}{5}$
c. $5\frac{4}{6} + \frac{5}{6}$	$\frac{7}{8} + 6\frac{4}{8}$
e. $\frac{7}{10} + 7\frac{9}{10}$	f. $9\frac{7}{12} + \frac{11}{12}$
$g. 2\frac{70}{100} + \frac{87}{100}$	h. $\frac{50}{100} + 16\frac{78}{100}$

5. To solve $7\frac{9}{10} + \frac{5}{10}$, Maria thought, " $7\frac{9}{10} + \frac{1}{10} = 8$ and $8 + \frac{4}{10} = 8\frac{4}{10}$." Paul thought, " $7\frac{9}{10} + \frac{5}{10} = 7\frac{14}{10} = 7 + \frac{10}{10} + \frac{4}{10} = 8\frac{4}{10}$." Explain why Maria and Paul are both right.



Name _____

Solve.

1.
$$3\frac{2}{5} + \underline{\hspace{1cm}} = 4$$

$$2. 2\frac{3}{8} + \frac{7}{8}$$



5			
	*		
	2		

Marta has 2 meters 80 centimeters of cotton cloth and 3 meters 87 centimeters of linen cloth. What is the total length of both pieces of cloth?									
			NA Luita o						
	Read	Draw	Write						



Lesson 31:

Add mixed numbers.

1. Solve.

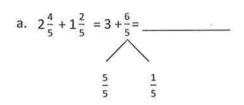
a.
$$3\frac{1}{3} + 2\frac{2}{3} = 5 + \frac{3}{3} =$$

$$3 \frac{1}{3} 2 \frac{2}{3}$$

b.
$$4\frac{1}{4} + 3\frac{2}{4}$$

c.
$$2\frac{2}{6} + 6\frac{4}{6}$$

2. Solve. Use a number line to show your work.





b.
$$1\frac{3}{4} + 3\frac{3}{4}$$

c.
$$3\frac{3}{8} + 2\frac{6}{8}$$

3. Solve. Use the arrow way to show how to make one.

$$a_{5} 2\frac{4}{6} + 1\frac{5}{6} = 3\frac{4}{6} + \frac{5}{6} =$$



- $b = 1\frac{3}{4} + 3\frac{3}{4}$
- c. $3\frac{3}{8} + 2\frac{6}{8}$
- 4. Solve. Use whichever method you prefer,
 - a. $1\frac{3}{5} + 3\frac{4}{5}$

b. $2\frac{6}{8} + 3\frac{7}{8}$

 $c = 3\frac{8}{12} + 2\frac{7}{12}$

Name _____ Date _____

Solve.

$$1. \ \ 2\frac{3}{8} + 1\frac{5}{8}$$

$$2. \ \ 3\frac{4}{5} + 2\frac{3}{5}$$



Meredith had 2 m 65 cm of ribbon. She used 87 cm of the ribbon. How much ribbon did she have left?

Read

Draw

Write



Lesson 32:

Subtract a fraction from a mixed number.

Date _____

1. Subtract. Model with a number line or the arrow way.

a.
$$3\frac{3}{4} - \frac{1}{4}$$

$$b. \quad 4\frac{7}{10} - \frac{3}{10}$$

c.
$$5\frac{1}{3} = \frac{2}{3}$$

d.
$$9\frac{3}{5} - \frac{4}{5}$$

2. Use decomposition to subtract the fractions. Model with a number line or the arrow way.

a.
$$5\frac{3}{5} - \frac{4}{5}$$

b.
$$4\frac{1}{4} - \frac{2}{4}$$

c.
$$5\frac{1}{3} - \frac{2}{3}$$

d.
$$2\frac{3}{8} - \frac{5}{8}$$

3. Decompose the total to subtract the fractions.

a.
$$3\frac{1}{8} - \frac{3}{8} = 2\frac{1}{8} + \frac{5}{8} = 2\frac{6}{8}$$

$$2\frac{1}{8}$$

$$b_1 5\frac{1}{8} - \frac{7}{8}$$

c.
$$5\frac{3}{5} - \frac{4}{5}$$

$$d. 5\frac{4}{6} - \frac{5}{6}$$

e.
$$6\frac{4}{12} - \frac{7}{12}$$

$$f_{\odot} 9\frac{1}{8} - \frac{5}{8}$$

g.
$$7\frac{1}{6} - \frac{5}{6}$$

h.
$$8\frac{3}{10} - \frac{4}{10}$$

i.
$$12\frac{3}{5} - \frac{4}{5}$$

j.
$$11\frac{2}{6} - \frac{5}{6}$$

Date _____

Solve.

1.
$$10\frac{5}{6} - \frac{4}{6}$$

2.
$$8\frac{3}{8} - \frac{6}{8}$$



	*		
			8

Jeannie's pumpkin had a we	ight of 3 kg 250 g i	n August and 4 kg	125 g in October. What was the
		agastana i ng	
difference in weight from Au	agust to October :		
	Read	Draw	Write



Lesson 33:

Subtract a mixed number from a mixed number.

Name	Date

1. Write a related addition sentence. Subtract by counting on. Use a number line or the arrow way to help. The first one has been partially done for you.

a.
$$3\frac{1}{3} - 1\frac{2}{3} =$$
______ $1\frac{2}{3} +$ _____ $= 3\frac{1}{3}$

b.
$$5\frac{1}{4} - 2\frac{3}{4} =$$

2. Subtract, as shown in Problem 2(a), by decomposing the fractional part of the number you are subtracting. Use a number line or the arrow way to help you.

a.
$$3\frac{1}{4} - 1\frac{3}{4} = 2\frac{1}{4} - \frac{3}{4} = 1\frac{2}{4}$$

$$\frac{1}{4} \quad \frac{2}{4}$$

$$b = 4\frac{1}{5} - 2\frac{4}{5}$$

c.
$$5\frac{3}{7} - 3\frac{6}{7}$$

3. Subtract, as shown in Problem 3(a), by decomposing to take one out.

a.
$$5\frac{3}{5} - 2\frac{4}{5} = 3\frac{3}{5} - \frac{4}{5}$$

$$2\frac{3}{5} \quad 1$$

b.
$$4\frac{3}{6} - 3\frac{5}{6}$$

c.
$$8\frac{3}{10} = 2\frac{7}{10}$$

4. Solve using any method.

a.
$$6\frac{1}{4} - 3\frac{3}{4}$$

b.
$$5\frac{1}{8} - 2\frac{7}{8}$$

c.
$$8\frac{3}{12} - 3\frac{8}{12}$$

d.
$$5\frac{1}{100} - 2\frac{97}{100}$$

Date _____

Solve using any strategy.

1.
$$4\frac{2}{3} = 2\frac{1}{3}$$

2.
$$12\frac{5}{8} - 8\frac{7}{8}$$



*			

There were $4\frac{1}{8}$ pizzas. Benny took $\frac{2}{8}$ of a pizza. How many pizzas are left?

Read

Draw

Write



Lesson 34:

Subtract mixed numbers.

1. Subtract.

a.
$$4\frac{1}{3} - \frac{2}{3}$$



b.
$$5\frac{2}{4} - \frac{3}{4}$$

c.
$$8\frac{3}{5} - \frac{4}{5}$$

2. Subtract the ones first.

a.
$$3\frac{1}{4} - 1\frac{3}{4} = 2\frac{1}{4} - \frac{3}{4} = 1\frac{2}{4}$$



b.
$$4\frac{2}{5} - 1\frac{3}{5}$$

c.
$$5\frac{2}{6} - 3\frac{5}{6}$$

d.
$$9\frac{3}{5} - 2\frac{4}{5}$$

3. Solve using any strategy.

a.
$$7\frac{3}{8} - 2\frac{5}{8}$$

b.
$$6\frac{4}{10} - 3\frac{8}{10}$$

c.
$$8\frac{3}{12} - 3\frac{8}{12}$$

d.
$$14\frac{2}{50} - 6\frac{43}{50}$$

Name _____

Solve.

1.
$$7\frac{1}{6} - 2\frac{4}{6}$$

2.
$$12\frac{5}{8} - 3\frac{7}{8}$$



Mary Beth is knitting scarves that are 1 meter long. If she knits 54 centimeters of a scarf each night for
3 nights, how many scarves will she complete? How much more does she need to knit to complete
another scarf?

Draw

Write

Lesson 35:

Read

1. Draw and label a tape diagram to show the following are true.

a. 8 fifths = $4 \times (2 \text{ fifths}) = (4 \times 2) \text{ fifths}$

b. $10 \text{ sixths} = 5 \times (2 \text{ sixths}) = (5 \times 2) \text{ sixths}$

- 2. Write the expression in unit form to solve.
 - a. $7 \times \frac{2}{3}$

b. $4 \times \frac{2}{4}$

c. $16 \times \frac{3}{8}$

d. $6 \times \frac{5}{8}$

- 3. Solve.
 - a. $7 \times \frac{4}{9}$

b. $6 \times \frac{3}{5}$

c. $8 \times \frac{3}{4}$

d. $16 \times \frac{3}{8}$

e. $12 \times \frac{7}{10}$

f. $3 \times \frac{54}{100}$

4. Maria needs $\frac{3}{5}$ yard of fabric for each costume. How many yards of fabric does she need for 6 costumes?

Name	Date	

1. Solve using unit form.

$$5 \times \frac{2}{3}$$

2. Solve.

$$11 \times \frac{5}{6}$$



Rhonda exercised for $\frac{5}{6}$ hour	every day for 5 day	ys. How many tota	Il hours did Rhonda exercise?	
	Read	Draw	Write	



Lesson 36:

Represent the multiplication of n times a/b as $(n \times a)/b$ using the associative property and visual models.

	H.		

1. Draw a tape diagram to represent

$$\frac{3}{4} + \frac{3}{4} + \frac{3}{4} + \frac{3}{4}$$

2. Draw a tape diagram to represent

$$\frac{7}{12} + \frac{7}{12} + \frac{7}{12}$$

Write a multiplication expression equal to

$$\frac{3}{4} + \frac{3}{4} + \frac{3}{4} + \frac{3}{4}$$

Write a multiplication expression equal to

$$\frac{7}{12} + \frac{7}{12} + \frac{7}{12}$$

3. Rewrite each repeated addition problem as a multiplication problem and solve. Express the result as a mixed number. The first one has been started for you.

$$a_1$$
 $\frac{7}{5} + \frac{7}{5} + \frac{7}{5} + \frac{7}{5} = 4 \times \frac{7}{5} = \frac{4 \times 7}{5} =$

b.
$$\frac{9}{10} + \frac{9}{10} + \frac{9}{10}$$

c.
$$\frac{11}{12} + \frac{11}{12} + \frac{11}{12} + \frac{11}{12} + \frac{11}{12}$$

- 4. Solve using any method. Express your answers as whole or mixed numbers.
 - a. $8 \times \frac{2}{3}$

b. $12 \times \frac{3}{4}$

c. $50 \times \frac{4}{5}$

d. $26 \times \frac{7}{8}$

5. Morgan poured $\frac{9}{10}$ liter of punch into each of 6 bottles. How many liters of punch did she pour in all?

6. A recipe calls for $\frac{3}{4}$ cup rice. How many cups of rice are needed to make the recipe 14 times?

7. A butcher prepared 120 sausages using $\frac{3}{8}$ pound of meat for each. How many pounds did he use in all?

Solve using any method.

1.
$$7 \times \frac{3}{4}$$

$$2. \quad 9 \times \frac{2}{5}$$

3.
$$60 \times \frac{5}{8}$$



The baker needs $\frac{5}{8}$ cup of rai	sins to make 1 bate	ch of cookies. How	w many cups of raisins do	es he need
to make 7 batches of cookie	s?			
9				
			#	
	Read	Draw	Write	



Lesson 37:

Find the product of a whole number and a mixed number using the distributive property.

Name	Date

1. Draw tape diagrams to show two ways to represent 2 units of $4\frac{2}{3}$.

Write a multiplication expression to match each tape diagram.

2. Solve the following using the distributive property. The first one has been done for you. (As soon as you are ready, you may omit the step that is in line 2.)

a.
$$3 \times 6\frac{4}{5} = 3 \times (6 + \frac{4}{5})$$

 $= (3 \times 6) + (3 \times \frac{4}{5})$
 $= 18 + \frac{12}{5}$
 $= 18 + 2\frac{2}{5}$
 $= 20\frac{2}{5}$

 $= 18 + 2\frac{1}{5}$ $= 20\frac{2}{5}$ c. $3 \times 2\frac{5}{8}$ d. $2 \times 4\frac{7}{10}$

e. $3 \times 7\frac{3}{4}$	
----------------------------	--

f. $6 \times 3\frac{1}{2}$

g.
$$4 \times 9\frac{1}{5}$$

h. $5\frac{6}{8} \times 4$

3. For one dance costume, Saisha needs $4\frac{2}{3}$ feet of ribbon. How much ribbon does she need for 5 identical costumes?

Name	Date
value	

Multiply. Write each product as a mixed number.

1.
$$4 \times 5\frac{3}{8}$$

2.
$$4\frac{3}{10} \times 3$$



Eight students are on a relay team. Each runs team run?	$1\frac{3}{4}$ kilometers.	How many total kilo	meters does their



Lesson 38:

Find the product of a whole number and a mixed number using the distributive property.

Draw

Write

Read

1. Fill in the unknown factors.

a.
$$7 \times 3\frac{4}{5} = (\underline{} \times 3) + (\underline{} \times \frac{4}{5})$$

b.
$$3 \times 12\frac{7}{8} = (3 \times \underline{\hspace{1cm}}) + (3 \times \underline{\hspace{1cm}})$$

2. Multiply. Use the distributive property.

a.
$$7 \times 8\frac{2}{5}$$

$$b_{10} 4\frac{5}{6} \times 9$$

c.
$$3 \times 8^{\frac{11}{12}}$$

d.
$$5 \times 20 \frac{8}{10}$$

e. $25\frac{4}{100} \times 4$

3. The distance around the park is $2\frac{5}{10}$ miles. Cecilia ran around the park 3 times. How far did she run?

4. Windsor the dog ate $4\frac{3}{4}$ snack bones each day for a week. How many bones did Windsor eat that week?

Date _____

1. Fill in the unknown factors.

$$8 \times 5\frac{2}{3} = (\underline{} \times 5) + (\underline{} \times \frac{2}{3})$$

2. Multiply. Use the distributive property.

$$6\frac{5}{8} \times 7$$

Name	Date
Use the RDW process to solve.	

1. Tameka ran $2\frac{5}{8}$ miles. Her sister ran twice as far. How far did Tameka's sister run?

2. Natasha's sculpture was $5\frac{3}{16}$ inches tall. Maya's was 4 times as tall. How much shorter was Natasha's sculpture than Maya's?

3. A seamstress needs $1\frac{5}{8}$ yards of fabric to make a child's dress. She needs 3 times as much fabric to make a woman's dress. How many yards of fabric does she need for both dresses?



Lesson 39:

Solve multiplicative comparison word problems involving fractions.

4. A piece of blue yarn is $5\frac{2}{3}$ yards long. A piece of pink yarn is 5 times as long as the blue yarn. Bailey tied them together with a knot that used $\frac{1}{3}$ yard from each piece of yarn. What is the total length of the yarn tied together?

5. A truck driver drove $35\frac{2}{10}$ miles before he stopped for breakfast. He then drove 5 times as far before he stopped for lunch. How far did he drive that day before his lunch break?

6. Mr. Washington's motorcycle needs $5\frac{5}{10}$ gallons of gas to fill the tank. His van needs 5 times as much gas to fill it. If Mr. Washington pays \$3 per gallon for gas, how much will it cost him to fill both the motorcycle and the van?

Name	Date	
(,		

Use the RDW process to solve.

Jeff has ten packages that he wants to mail. Nine identical packages weigh $2\frac{7}{8}$ pounds each. A tenth package weighs two times as much as one of the other packages. How many pounds do all ten packages weigh?



Lesson 39:

Solve multiplicative comparison word problems involving fractions.

Height

M=	Data
Name	Date

- 1. The chart to the right shows the height of some football players.
 - a. Use the data to create a line plot at the bottom of this page and to answer the questions below.
 - b. What is the difference in height of the tallest and shortest players?

c. Player I and Player B have a combined height that is $1\frac{1}{8}$ feet taller than a school bus. What is the height of a school bus?

Player	(in feet)
А	6 1/4
В	5 7 8
С	6 1
D	6 1/4
E	6 2
F	57/8
G	6 1/8
Н	6 5
t	5 6 8
J	6\frac{1}{8}

2. One of the players on the team is now 4 times as tall as he was at birth, when he measured $1\frac{5}{8}$ feet. Who is the player?

3. Six of the players on the team weigh over 300 pounds. Doctors recommend that players of this weight drink at least $3\frac{3}{4}$ quarts of water each day. At least how much water should be consumed per day by all 6 players?

4. Nine of the players on the team weigh about 200 pounds. Doctors recommend that people of this weight each eat about $3\frac{7}{10}$ grams of carbohydrates per pound each day. About how many combined grams of carbohydrates should these 9 players eat per pound each day?

Name	Date

Coach Taylor asked his team to record the distance they ran during practice.

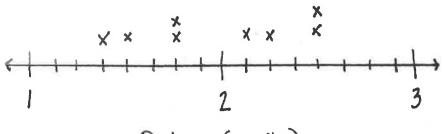
The distances are listed in the table.

1. Use the table to locate the incorrect data on the line plot.

Circle any incorrect points.

Mark any missing points.

Diotance Ran During Practice



Distance (in miles)

X=1 team member

2.	Of the team members who ran $1\frac{6}{8}$ miles, how many miles did those
	team members run combined?

Team Members	Distance (in miles)
Alec	13/4
Henry	1 1 2
Charles	2 1 8
Steve	13/4
Pitch	2 2/4
Raj	1 <mark>6</mark>
Pam	$2\frac{1}{2}$
Tony	1 3 8

Jackie's paper chain was 5 times as long as Sammy's, which measured $2\frac{75}{100}$ meters.	What was the
total length of both their chains?	

Read

Draw

Write



Lesson 41:

Find and use a pattern to calculate the sum of all fractional parts between 0 and 1. Share and critique peer strategies.

ÿ.

Name _____

Date _____

1. Find the sums.

a.
$$\frac{0}{3} + \frac{1}{3} + \frac{2}{3} + \frac{3}{3}$$

b.
$$\frac{0}{4} + \frac{1}{4} + \frac{2}{4} + \frac{3}{4} + \frac{4}{4}$$

C.
$$\frac{0}{5} + \frac{1}{5} + \frac{2}{5} + \frac{3}{5} + \frac{4}{5} + \frac{5}{5}$$

$$\mathbf{d}_{\bullet} \quad \frac{0}{6} + \frac{1}{6} + \frac{2}{6} + \frac{3}{6} + \frac{4}{6} + \frac{5}{6} + \frac{6}{6}$$

e.
$$\frac{0}{7} + \frac{1}{7} + \frac{2}{7} + \frac{3}{7} + \frac{4}{7} + \frac{5}{7} + \frac{6}{7} + \frac{7}{7}$$

f.
$$\frac{0}{8} + \frac{1}{8} + \frac{2}{8} + \frac{3}{8} + \frac{4}{8} + \frac{5}{8} + \frac{6}{8} + \frac{7}{8} + \frac{8}{8}$$

2. Describe a pattern you notice when adding the sums of fractions with even denominators as opposed to those with odd denominators.

3. How would the sums change if the addition started with the unit fraction rather than with 0?

4. Find the sums.

a.
$$\frac{0}{10} + \frac{1}{10} + \frac{2}{10} + \dots + \frac{10}{10}$$

b.
$$\frac{0}{12} + \frac{1}{12} + \frac{2}{12} + \frac{12}{12} + \frac{12}{12}$$

C.
$$\frac{0}{15} + \frac{1}{15} + \frac{2}{15} + \dots + \frac{15}{15}$$

d.
$$\frac{0}{25} + \frac{1}{25} + \frac{2}{25} + \dots + \frac{25}{25}$$

e.
$$\frac{0}{50} + \frac{1}{50} + \frac{2}{50} + \cdots + \frac{50}{50}$$

f.
$$\frac{0}{100} + \frac{1}{100} + \frac{2}{100} + \dots + \frac{100}{100}$$

5. Compare your strategy for finding the sums in Problems 4(d), 4(e), and 4(f) with a partner.

6. How can you apply this strategy to find the sum of all the whole numbers from 0 to 100?

Name _____ Date _____

Find the sums.

1.
$$\frac{0}{20} + \frac{1}{20} + \frac{2}{20} + \dots + \frac{20}{20}$$

2.
$$\frac{0}{200} + \frac{1}{200} + \frac{2}{200} + \dots + \frac{200}{200}$$

Credits

Great Minds® has made every effort to obtain permission for the reprinting of all copyrighted material. If any owner of copyrighted material is not acknowledged herein, please contact Great Minds for proper acknowledgment in all future editions and reprints of this module.



Module 5:

Credits

27								
			+					
7.								

		N		
	*			
			Á	